GCSE MATHS Aiming for Grade 9 REVISION BOOKLET



2018 Exam Dates:

24th May 2018 7th June 2018 12th June at 2018

Name:

Contents

	Page:
Number:	-
Surds	3
Algebraic proofs	7
Algebra:	
Transformations of graphs	13
Equations of circles	17
Quadratic and other sequences	19
Completing the square	22
Inverse and composite functions	25
Expanding more than two binomials	28
Nonlinear simultaneous equations	30
Solving quadratic inequalities	34
Shape, Space and Measure:	
Circle theorems	36
Vectors	40
Sine and cosine rules	48
Area under graphs	52
Data Handling:	
Histograms	57
Moving averages	65
Probability:	
Set theory	68
Ratio and Proportion:	
Proportion	71
Percentages – reverse	75

<u>Surds</u>

Things to remember:

- $\sqrt{\text{means square root}};$
- To simplify surds, find all its factors;
- To rationalise the denominator, find an equivalent fraction where the denominator is rational.

Questions:

1. Work out

$$(5+\sqrt{3})(5-\sqrt{3})$$

 $\sqrt{22}$ Give your answer in its simplest form.

(Total 3 marks)

2. (a) Rationalise the denominator of $\frac{1}{\sqrt{3}}$

(1)

(b) Expand $(2 + \sqrt{3})(1 + \sqrt{3})$ Give your answer in the form $a + b\sqrt{3}$ where *a* and *b* are integers.

> (2) (Total 3 marks)

3. (a) Rationalise the denominator of $\frac{1}{\sqrt{7}}$

(b) (i) Expand and simplify $(\sqrt{3} + \sqrt{15})^2$ Give your answer in the form $a + b\sqrt{3}$ where *a* and *b* are integers.

(ii) All measurements on the triangle are in centimetres.
 ABC is a right-angled triangle.
 k is a positive integer.

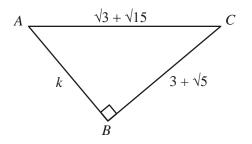


Diagram **NOT** accurately drawn

Find the value of k.

k =(5) (Total 7 marks)

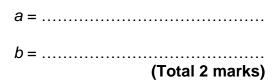
(2)

4. Expand and simplify $(\sqrt{3} - \sqrt{2})(\sqrt{3} - \sqrt{2})$

			(Total 2 marks)
5.	(a)	Write down the value of $49^{1/2}$	
	(b)	Write $\sqrt{45}$ in the form $k\sqrt{5}$, where k is an integer.	(1)

(1) (Total 2 marks)

6. Write
$$\frac{\sqrt{18} + 10}{\sqrt{2}}$$
 in the form $a + b\sqrt{3}$ where *a* and *b* are integers.



7. Expand and simplify $(2 + \sqrt{3})(7 - \sqrt{3})$ Give your answer in the form $a + b\sqrt{3}$ where *a* and *b* are integers.

(Total 3 marks)

8. Rationalise the denominator of $\frac{4 + \sqrt{2}(4 - \sqrt{2})}{\sqrt{7}}$ Give your answer in its simplest form.

(Total for question = 3 marks)

9. Show that $\frac{4-\sqrt{3}(4+\sqrt{3})}{\sqrt{13}}$ simplifies to $\sqrt{13}$

(Total for question = 2 marks)

Algebraic Proofs

Things to remember:

- Start by expanding the brackets, then factorise.
- Remember the following:
 - **1.** $2n \rightarrow even number$
 - **2.** $2n + 1 \rightarrow odd$ number
 - 3. $a(bn + c) \rightarrow multiple of a$
 - 4. Consecutive numbers are numbers that appear one after the other.

Questions:

1. (a) Expand and simplify x(x + 1)(x - 1)

(2) In a list of three consecutive positive integers at least one of the numbers is even and one of the numbers is a multiple of 3

n is a positive integer greater than 1

(b) Prove that $n^3 - n$ is a multiple of 6 for all possible values of n.

261 – 1 is a prime number.

(c) Explain why 261 + 1 is a multiple of 3

(2)

.....

2. Prove that

 $(2n + 3)^2 - (2n - 3)^2$ is a multiple of 8 for all positive integer values of n.

(Total for Question is 3 marks)

3. (a) Expand and simplify (y - 2)(y - 5)

(2)

*(b) Prove algebraically that $(2n + 1)^2 - (2n + 1)$ is an even number for all positive integer values of n.

(3) (Total for Question is 5 marks)

4. * Prove algebraically that the difference between the squares of any two consecutive integers is equal to the sum of these two integers.

(Total for Question is 4 marks) (a) Factorise $x^2 + 7x$ 5. (1) Factorise $y^2 - 10y + 16$ (b) (2) *(C) (i) Factorise $2t^2 + 5t + 2$ t is a positive whole number. (ii) The expression $2t^2 + 5t + 2$ can never have a value that is a prime number. Explain why. (3)

(Total for Question is 6 marks)

(b) (i) Expand and simplify 7(2x + 1) + 6(x + 3)

(ii) Show that when x is a whole number 7(2x + 1) + 6(x + 3) is always a multiple of 5

(3) (Total for Question is 4 marks)

.....

(1)

7. Prove that $(n - 1)^2 + n^2 + (n + 1)^2 = 3n^2 + 2$

(Total for Question is 2 marks)

8. Prove algebraically that the difference between the squares of any two consecutive integers is equal to the sum of these two integers.

(Total for question is 4 marks)

9. The product of two consecutive positive integers is added to the larger of the two integers. Prove that the result is always a square number.

(Total for question = 3 marks)

10. Prove algebraically that $(2n + 1)^2 - (2n + 1)$ is an even number for all positive integer values of n.

(Total for question = 3 marks)

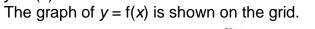
Transformations of graphs

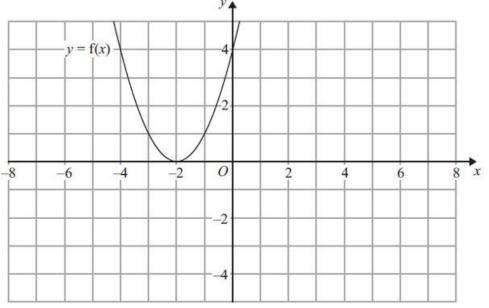
Things to remember:

- 1. f(x) means the function of x.
- 2. -f(x) is a reflection in the x-axis.
- 3. f(-x) is a reflection in the y-axis.
- 4. f(x a) is a translation in the x-axis, a units.
- 5. f(x) + b is a translation in the y-axis, b units.
- 6. cf(x) is an enlargement in the y-axis, scale factor c.
- 7. f(dx) is an enlargement in the x-axis, scale factor $\frac{1}{d}$.

Questions:

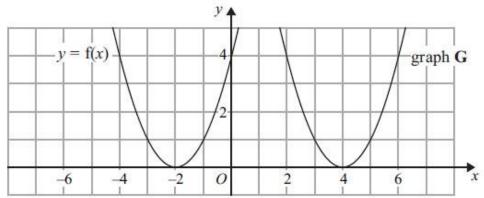
1. y = f(x)





(a) On the grid above, sketch the graph of y = -f(x).

The graph of y = f(x) is shown on the grid.



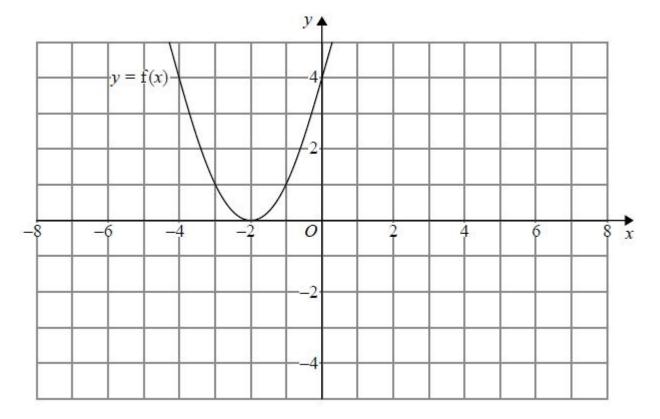
The graph **G** is a translation of the graph of y = f(x).

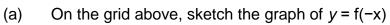
(b) Write down the equation of graph **G**.

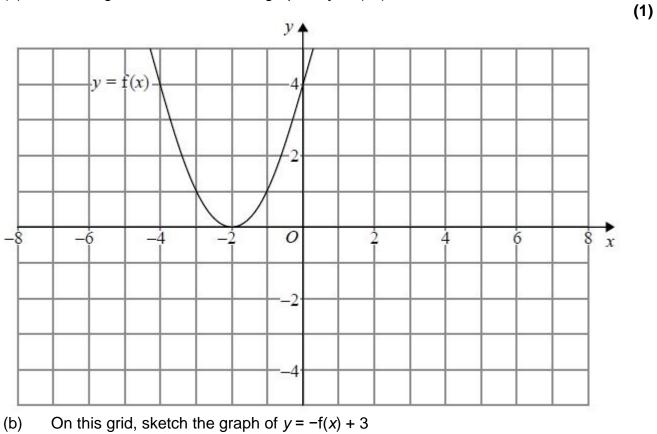
(2) (Total for Question is 3 marks)

(2)

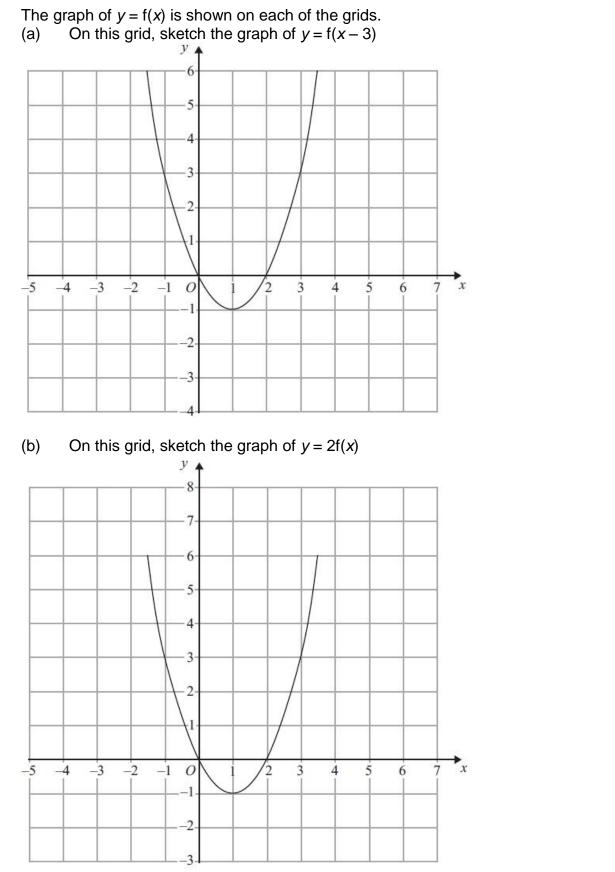
2. The graph of y = f(x) is shown on both grids below.







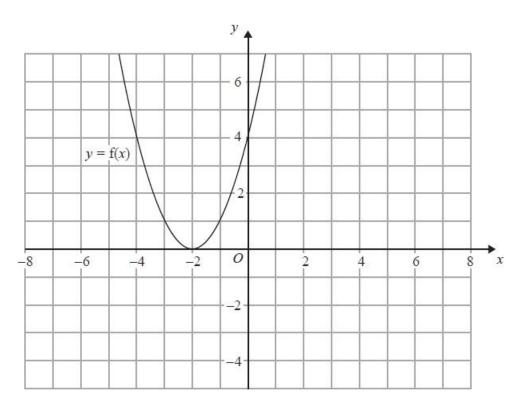
(1) (Total for question = 2 marks)



3.

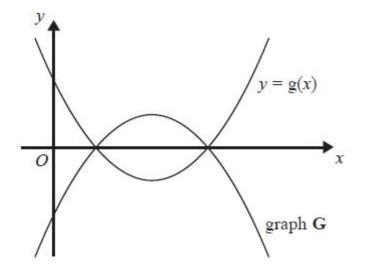
(2) (Total for Question is 4 marks)

(2)



(a) On the grid above, sketch the graph of y = f(x + 3)

The graph of y = g(x) is shown below.



The graph **G** is the reflection of y = g(x) in the *x*-axis. (b) Write down an equation of graph **G**.

> (1) (Total for question = 3 marks)

(2)

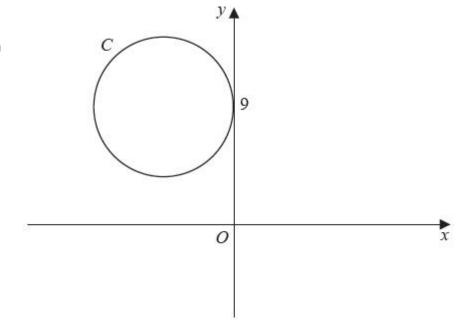
Equations of Circles

Things to remember:

- 8. The general equation of a circle is $(x a)^2 + (y b)^2 = r^2$, where (a, b) is the centre and r is the radius.
- 9. To calculate the equation of the tangent:
 - 1. Calculate the gradient of the radius of the circle.
 - 2. Calculate the gradient of the tangent of the circle.
 - 3. Substitute the given coordinate and the gradient of the tangent into y = mx + c to calculate the y-intercept.

Questions:

- 1. The circle C has radius 5 and touches the y-axis at the point (0, 9), as shown in the diagram.
 - (a) Write down an equation for the circle C, that is shown in the diagram.



(3)

A line through the point P(8, -7) is a tangent to the circle C at the point T. (b) Find the length of PT.

> (3) (Total 6 marks)

2. A circle C has centre (-1, 7) and passes through the point (0, 0). Find an equation for C.

.....

(Total 4 marks)

The circle C has centre (3, 1) and passes through the point P(8, 3).
(a) Find an equation for C.

(b) Find an equation for the tangent to C at P. (4)

.....

(5) (Total 9 marks)

Quadratic and Other Sequences

Things to remember:

- To calculate the nth term of a quadratic sequence:
 - 1. Calculate the first difference.
 - 2. Calculate the second difference.
 - 3. How many n²s?
 - 4. Subtract.

1

- 5. Calculate the nth term of the difference.
- 6. Write the quadratic nth term.

Questions:

1. Here are the first 5 terms of a quadratic sequence.

3 7 13 21

Find an expression, in terms of *n*, for the *n*th term of this quadratic sequence.

(Total for question is 3 marks)

Here are the first six terms of a Fibonacci sequence.
 1
 1
 2
 3
 5
 8
 The rule to continue a Fibonacci sequence is,

- the next term in the sequence is the sum of the two previous terms.
- (a) Find the 9th term of this sequence.

.....

The first three terms of a different Fibonacci sequence are

a b a+b

(b) Show that the 6th term of this sequence is 3a + 5b

(1)

Given that the 3rd term is 7 and the 6th term is 29,

(c) find the value of *a* and the value of *b*.

a = *b* = (3) (Total for question = 6 marks) Here are the first five terms of a sequence. 3. 18 2 8 32 50 Find the next term of this sequence. (a) (1) The *n*th term of a different sequence is $3n^2 - 10$ Work out the 5th term of this sequence. (b)

> (1) (Total for question = 2 marks)

- 4. Here are the first five terms of an arithmetic sequence. 1 5 9 13 17
 - (a) Write down an expression, in terms of *n*, for the *n*th term of this sequence.

.....

(2)

The *n*th term of a different number sequence is $3n^2 + 7$ (b) Find the 10th term of this sequence.

(Total for Question is 4 marks)

Completing the Square

Things to remember:

- To complete the square:
 - 1. Halve the coefficient of x.
 - 2. Put in brackets with the x and square the brackets.
 - 3. Subtract the half-coefficient squared.
 - 4. Don't forget the constant on the end!
 - 5. Simply.
- For $(x p)^2 + q = 0$, the turning point is (p, q).

Questions:

1. (i) Sketch the graph of $f(x) = x^2 - 5x + 10$, showing the coordinates of the turning point and the coordinates of any intercepts with the coordinate axes.

(ii) Hence, or otherwise, determine whether f(x + 2) - 3 = 0 has any real roots. Give reasons for your answer.

(Total for question = 6 marks)

2. (a) Write $2x^2 + 16x + 35$ in the form $a(x + b)^2 + c$ where a, b, and c are integers.

.....

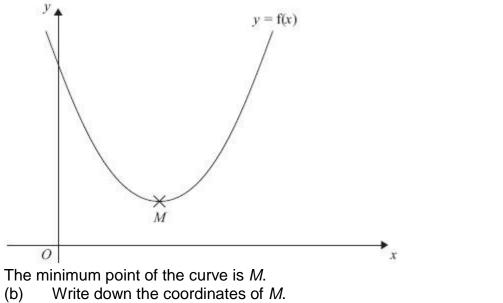
(3)

(b) Hence, or otherwise, write down the coordinates of the turning point of the graph of $y = 2x^2 + 16x + 35$

(1) (Total for question = 4 marks)

3. The expression $x^2 - 8x + 21$ can be written in the form $(x - a)^2 + b$ for all values of x. (a) Find the value of a and the value of b.

The equation of a curve is y = f(x) where $f(x) = x^2 - 8x + 21$ The diagram shows part of a sketch of the graph of y = f(x).



(1)

(Total for Question is 4 marks)

Inverse and Composite Functions

Things to remember:

- y = f(x) means that y is a function of x.
- f(a) means the value of x is a, so substitute x with a.
- The graph of the inverse is the reflection of the graph in the line y = x
- We find the inverse function by putting the original function equal to y and rearranging to make x the subject.
- We use the notation f-1(x) for the inverse function.
- When a function is followed by another, the result is a composite function.
- fg(x) means do g first, followed by f.

Questions:

- 1. The functions f and g are such that
 - f(x) = 1 5x and g(x) = 1 + 5x
 - (a) Show that gf(1) = -19

(b) Prove that $f^{-1}(x) + g^{-1}(x) = 0$ for all values of *x*.

(3) (Total for question = 5 marks)

(2)

- 2. The function f is such that f(x) = 4x - 1
 - Find $f^{-1}(x)$ (a)

 $f^{-1}(x) = \dots$ (2)

The function g is such that $g(x) = kx^2$ where k is a constant. Given that fg(2) = 12work out the value of k (b)

> *k* = (2) (Total for question = 4 marks)

- The functions f and g are such that 3. f(x) = 3(x - 4) and $g(x) = \frac{x}{5} + 1$ Find the value of f(10)
 - (a)

(b) Find $g^{-1}(x)$

(1)

.....

(c) Show that ff(x) = 9x - 48

(2) (Total for question = 5 marks)

4. $f(x) = 3x^2 - 2x - 8$ Express f(x + 2) in the form $ax^2 + bx$

(Total for question is 3 marks)

Expanding more than two binomials

Things to remember:

- Start by expanding two pair of brackets using the grid or FOIL method.
- Then expand the third set of brackets.
- Use columns to keep x^3 , x^2 etc in line to help with addition.

Questions:

1. Show that $(x - 1)(x + 2)(x - 4) = x^3 - 3x^2 - 6x + 8$ for all values of x.

.....

(Total for question is 3 marks)

2. Show that $(3x - 1)(x + 5)(4x - 3) = 12x^3 + 47x^2 - 62x + 15$ for all values of x.

(Total for question is 3 marks)

3. Show that $(x - 3)(2x + 1)(x + 3) = 2x^3 + x^2 - 18x - 9$ for all values of x.

(Total for question is 3 marks)

4. $(2x + 1)(x + 6)(x - 4) = 2x^3 + ax^2 + bx - 24$ for all values of x, where a and b are integers. Calculate the values of a and b.

> a = b = (Total for question is 4 marks)

Nonlinear Simultaneous Equations

Things to remember:

- 1. Substitute the linear equation into the nonlinear equation.
- 2. Rearrange so it equals 0.
- 3. Factorise and solve for the first variable (remember there will be two solutions).
- 4. Substitute the first solutions to solve for the second variable.
- 5. Express the solution as a pair of coordinate where the graphs intersect.

Questions:

1. Solve the equations

$$x^{2} + y^{2} = 36$$

 $x = 2y + 6$

(Total for Question is 5 marks)

3. Solve the simultaneous equations $x^{2} + y^{2} = 25$ y = 2x + 5

4. Solve the simultaneous equations

$$x^{2} + y^{2} = 9$$
$$x + y = 2$$

Give your answers correct to 2 decimal places.

 5. Solve algebraically the simultaneous equations $x^{2} + y^{2} = 25$ y - 2x = 5

(Total for Question is 5 marks)

Solving Quadratic Inequalities

Things to remember:

• Start by solving the quadratic to find the values of x, then sketch the graph to determine the inequality.

Questions:

1. Solve $x^2 > 3x + 4$

(Total for question = 3 marks)

2. Solve the inequality $x^2 > 3(x+6)$

(Total for question = 4 marks)

3. Solve the inequality $x^2 + 5x > 6$

(Total for question = 3 marks)

4. Solve the inequality $x^2 - 2x + 8 < 0$

(Total for question = 3 marks)

5. Solve the inequality $x^2 - x \ge 12$

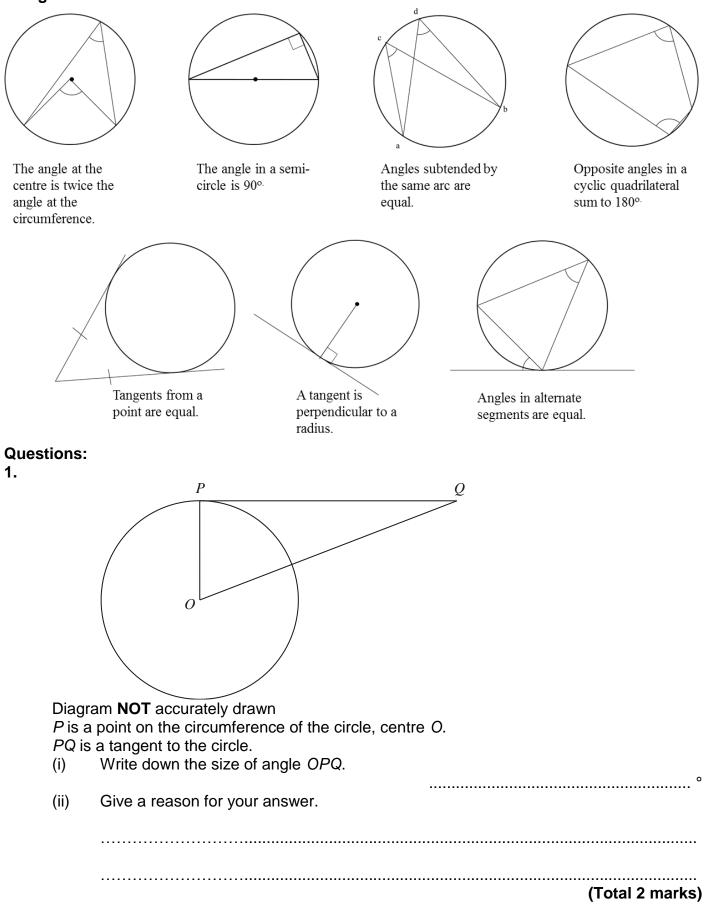
(Total for question = 3 marks)

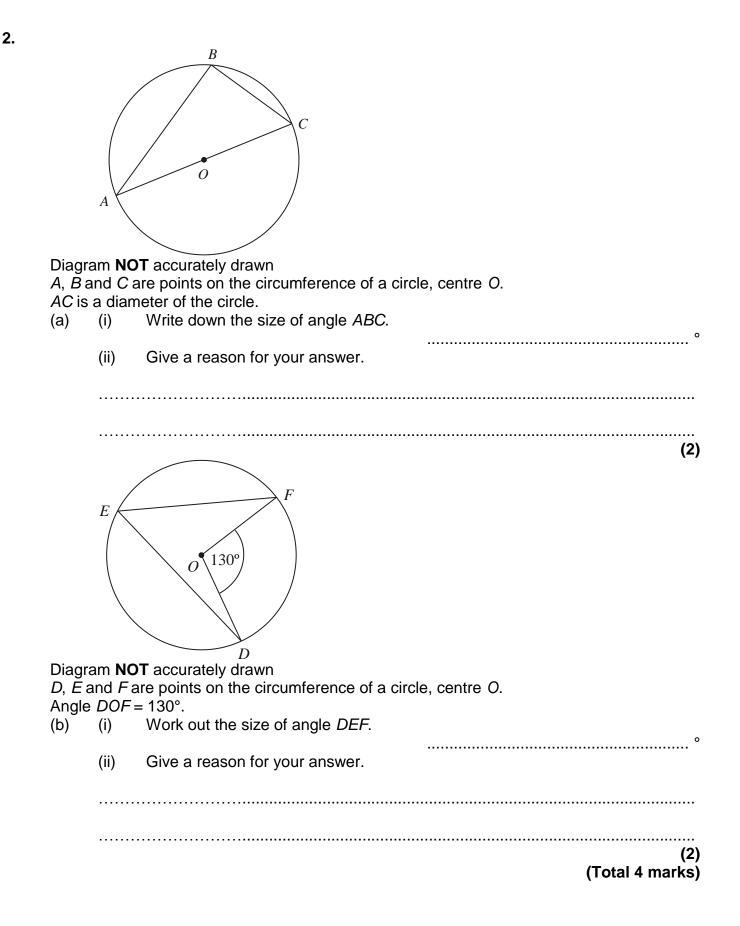
6. Solve the inequality $x^2 \le 4(2x + 5)$

(Total for question = 4 marks)

Circle theorems

Things to remember:





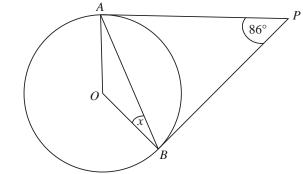


Diagram **NOT** accurately drawn A and B are points on the circumference of a circle, centre O. PA and PB are tangents to the circle. Angle APB is 86°. Work out the size of the angle marked x.

o	

(Total 2 marks)



3.

A	$ \begin{array}{c} 70^{\circ} \\ 0 \\ x^{\circ} \\ y^{\circ} \\ B \end{array} $	
	$P = X^{\circ}.$	0.
(u) (i) (ii)	Give a reason for your answer.	٥
.,	·	
(b) (i)	Work out the value of <i>y</i> .	(2)
(ii)	Give a reason for your answer.	٥
	(Tota	(2) al 4 marks)

.

The diagram A, B and C DCO is a si DA is a tan	gent to the circle.	D
Angle ADO (a) Wor	$P = 36^{\circ}$ k out the size of angle AOD.	
(b) (i)	Work out the size of angle <i>ABC</i> .	。 (2)
(ii)	Give a reason for your answer.	
		(3) (Total 5 marks)

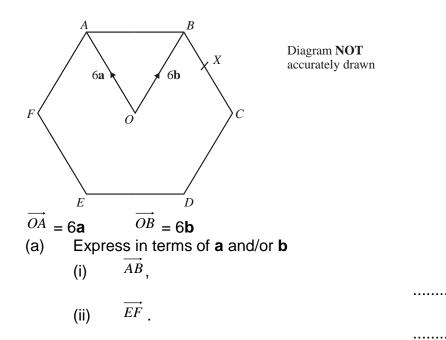
Vectors

Things to remember:

- Use the letter provided in the question.
- Going against the arrow is a negative.
- Vectors need to be written in bold or underlined.
- They can be manipulated similarly to algebra.

Questions:

1. The diagram shows a regular hexagon *ABCDEF* with centre *O*.



X is the midpoint of BC.

(b) Express \overrightarrow{EX} in terms of **a** and/or **b**

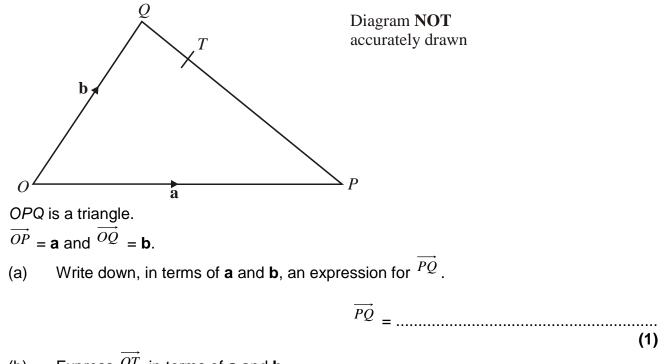
.....

(2)

Y is the point on AB extended, such that AB : BY = 3:2

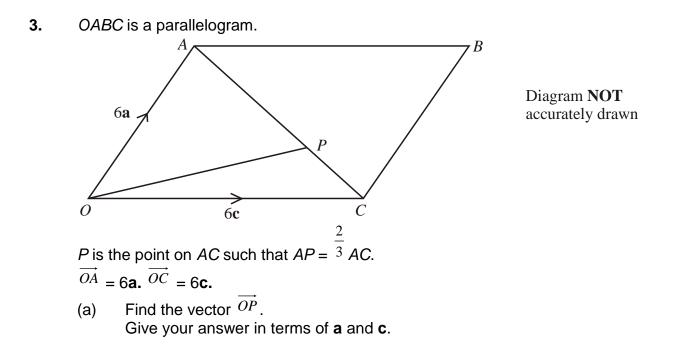
(c) Prove that *E*, *X* and *Y* lie on the same straight line.

(3) (Total 7 marks)



(b) Express \overrightarrow{OT} in terms of **a** and **b**. Give your answer in its simplest form.

 \overrightarrow{OT} =(2) (Total 3 marks)



The midpoint of *CB* is *M*.(b) Prove that *OPM* is a straight line.

(2) (Total 5 marks)

.....

(3)

4. OPQ is a triangle. R is the midpoint of OP. S is the midpoint of PQ. $\overrightarrow{OP} = \mathbf{p}$ and $\overrightarrow{OQ} = \mathbf{q}$

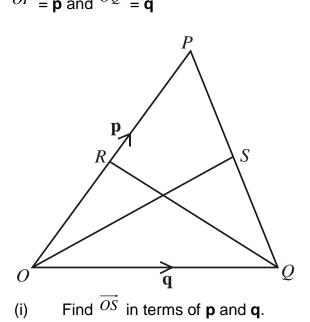
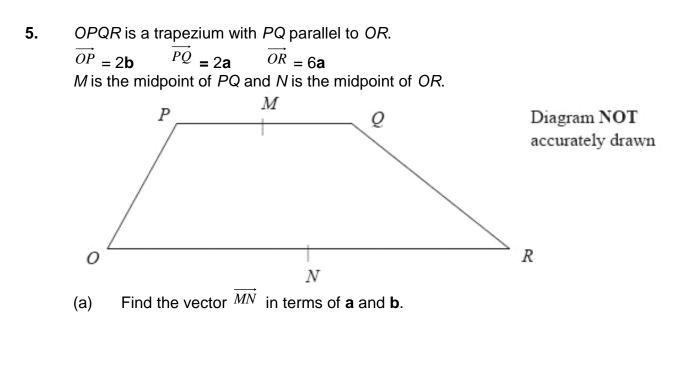


Diagram **NOT** accurately drawn

(ii) Show that *RS* is parallel to *OQ*.



(Total 5 marks)

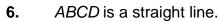


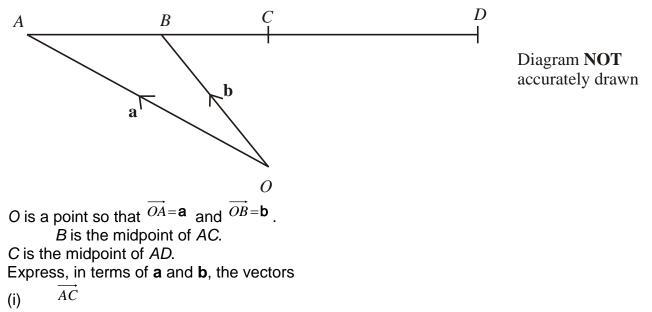


X is the midpoint of *MN* and Y is the midpoint of *QR*.

(b) Prove that XY is parallel to OR.

(2) (Total 4 marks)

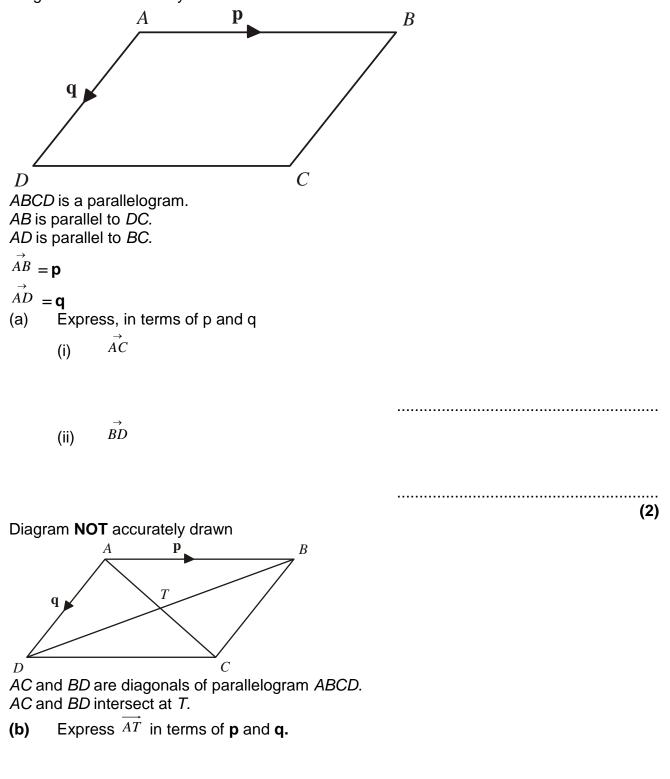




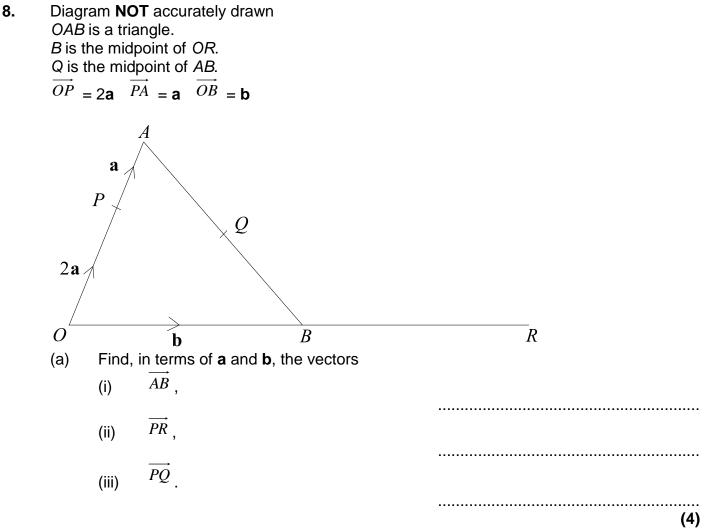
(ii) <u>*OD*</u>

.....

(Total 3 marks)



(1) (Total 3 marks)



(b) Hence explain why *PQR* is a straight line.

The length of *P*Q is 3 cm. (c) Find the length of *PR*. (2)

..... cm (1) (Total 7 marks)

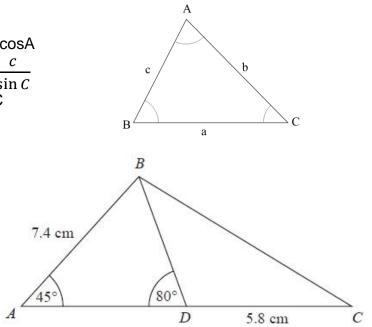
Sine and Cosine Rules

Things to remember:

- For any triangle ABC, $a^2 = b^2 + c^2 2bc \cos A$
- For any triangle ABC, $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$
- For any triangle ABC, area = $\frac{1}{2}$ a b sinC

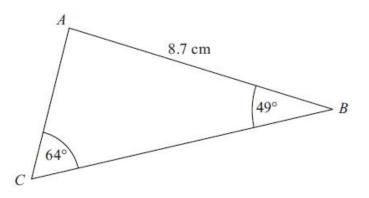
Questions:

1. Diagram **NOT** accurately drawn *ABC* is a triangle. *D* is a point on *AC*. Angle $BAD = 45^{\circ}$ Angle $ADB = 80^{\circ}$ AB = 7.4 cm DC = 5.8 cmWork out the length of *BC*. Give your answer correct to 3 significant figures.

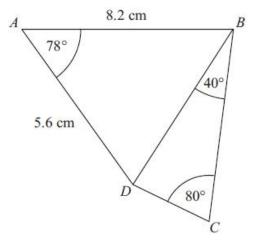


..... cm (Total for question = 5 marks)

2. Diagram **NOT** accurately drawn *ABC* is a triangle. *AB* = 8.7 cm. Angle $ABC = 49^{\circ}$. Angle $ACB = 64^{\circ}$. Calculate the area of triangle *ABC*. Give your answer correct to 3 significant figures.

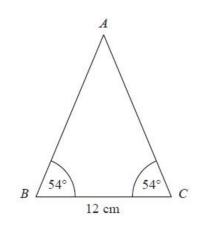


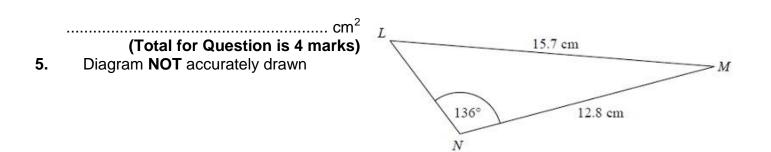
 ABCD is a quadrilateral. Diagram NOT accurately drawn Work out the length of DC. Give your answer correct to 3 significant figures.



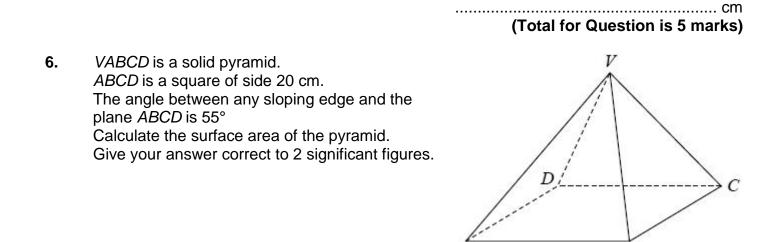
..... cm (Total for Question is 6 marks)

 Diagram NOT accurately drawn ABC is an isosceles triangle. Work out the area of the triangle. Give your answer correct to 3 significant figures.





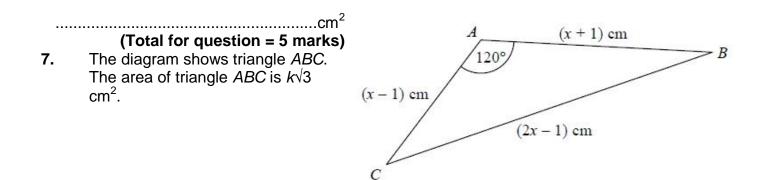
The diagram shows triangle LMN. Calculate the length of LN. Give your answer correct to 3 significant figures.



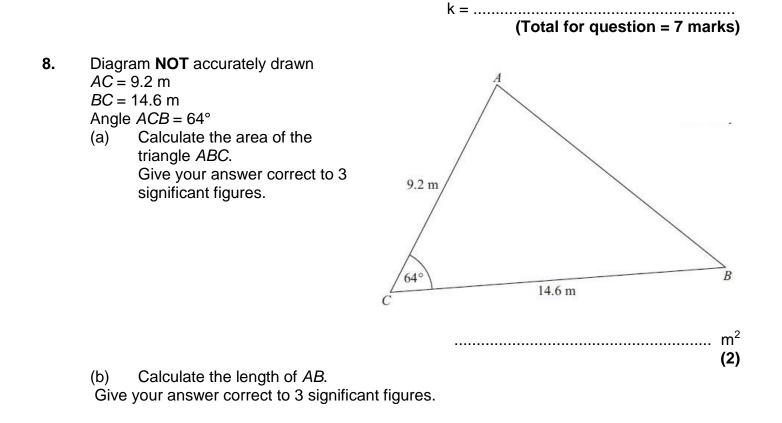
20 cm

A

В



Find the exact value of *k*.



(Total for Question is 5 marks)

.....

(3)

Area under Graphs

Things to remember:

- Velocity is speed with direction
- Acceleration and deceleration is given by the gradient of the graph $\left(\frac{rise}{run}\right)$
- The distance travelled is given by the area under the graph.

Questions:

1. A car has an initial speed of u m/s.

The car accelerates to a speed of 2u m/s in 12 seconds.

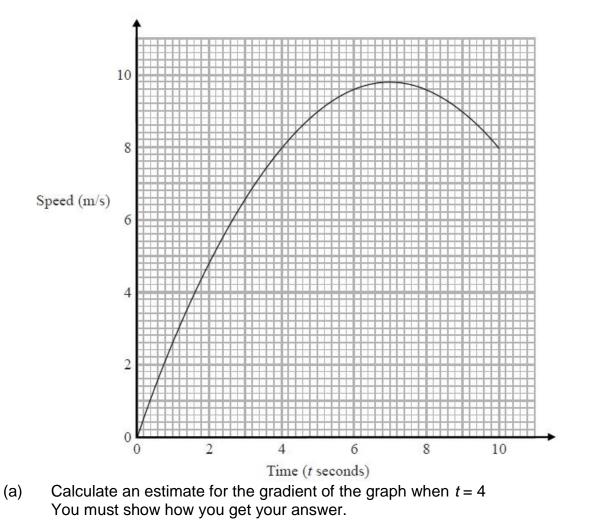
The car then travels at a constant speed of 2u m/s for 10 seconds.

Assuming that the acceleration is constant, show that the total distance, in metres, travelled by the car is 38*u*.

(Total for question = 4 marks)

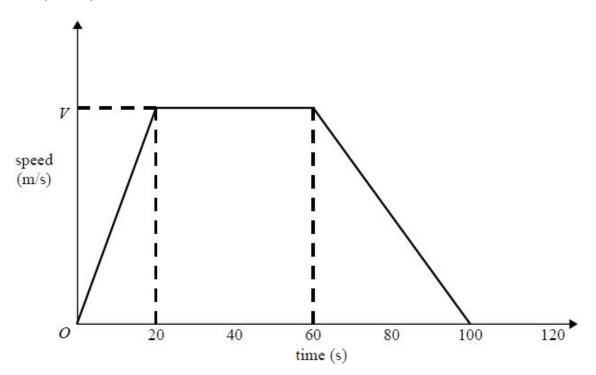
2. Karol runs in a race.

The graph shows her speed, in metres per second, *t* seconds after the start of the race.



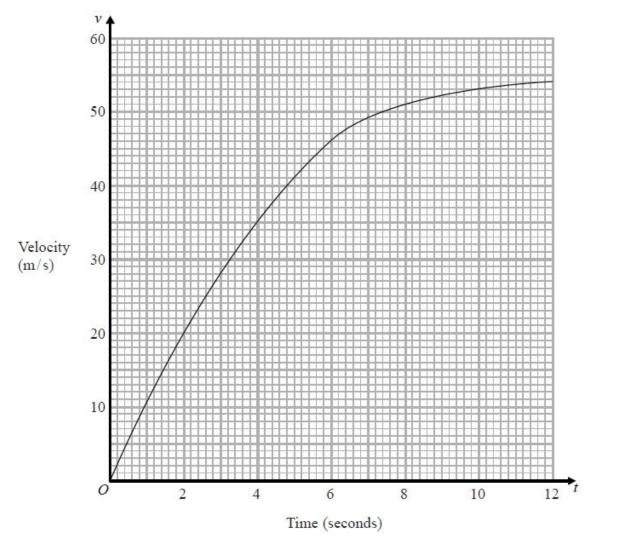
(b)	Describe fully what your answer to part (a) represents.	 (3)
(c)	Explain why your answer to part (a) is only an estimate.	 (2)
	(Total for question = 6 mark	 (1) (s)

3. Here is a speed-time graph for a car journey. The journey took 100 seconds.



The car travelled 1.75km in the 100 seconds. (a) Work out the value of *V*.

(b) Describe the acceleration of the car for each part of this journey. (3) 4. The graph shows information about the velocity, *v* m/s, of a parachutist *t* seconds after leaving a plane.

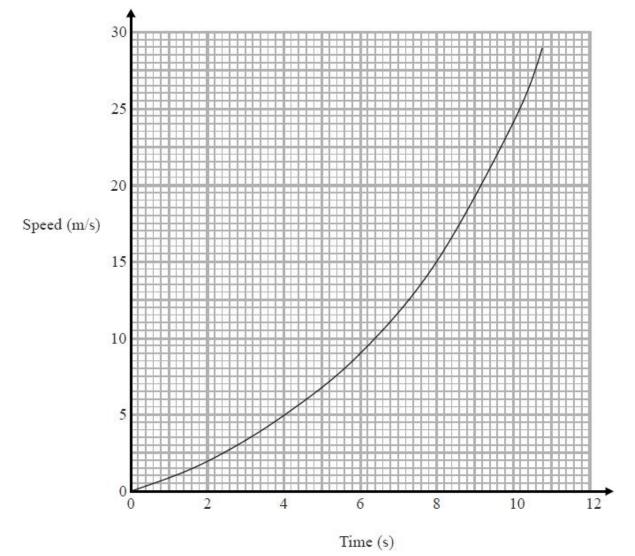


(a) Work out an estimate for the acceleration of the parachutist at t = 6

(b) Work out an estimate for the distance fallen by the parachutist in the first12 seconds after leaving the plane.Use 3 strips of equal width.

..... m (3)

(Total for question is 5 marks)



(a) Work out an estimate for the distance the car travelled in the first 10 seconds. Use 5 strips of equal width.

(b) Is your answer to (a) an underestimate or an overestimate of the actual distance? Give a reason for your answer. (1) (Total for question = 4 marks)

Histograms

Things to remember:

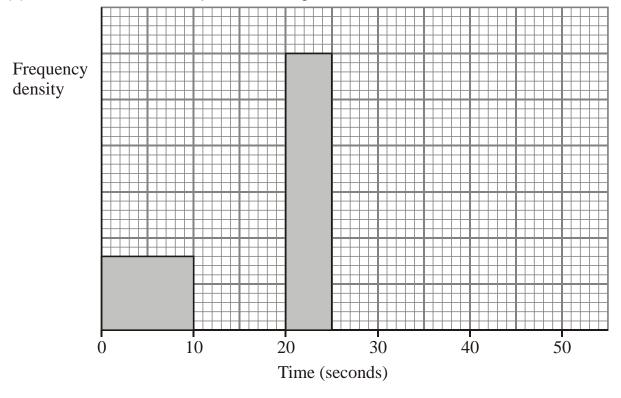
- Frequency = Frequency Density x Class Width;
- The y-axis will always be labelled "frequency density";
- The x-axis will have a continuous scale.

Questions:

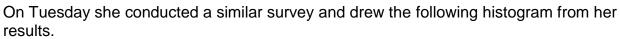
1. One Monday, Victoria measured the time, in seconds, that individual birds spent on her bird table. She used this information to complete the frequency table.

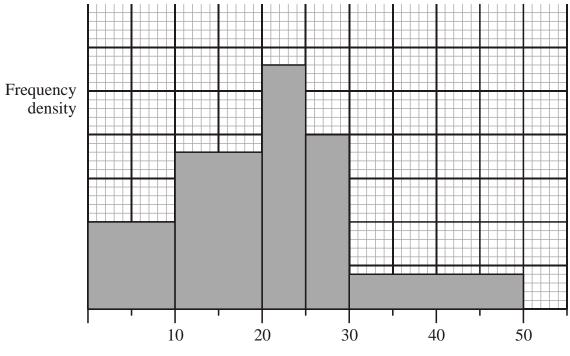
Time (t seconds)	Frequency
0 < <i>t</i> ≤ 10	8
10 < <i>t</i> ≤ 20	16
20 < <i>t</i> ≤ 25	15
25 < <i>t</i> ≤ 30	12
30 < <i>t</i> ≤ 50	6

(a) Use the table to complete the histogram.



(3)



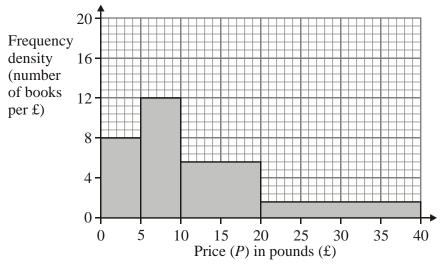


Time (Seconds)

(b) Use the histogram for Tuesday to complete the table.

Time (t seconds)	Frequency
0 < <i>t</i> ≤ 10	10
10 < <i>t</i> ≤ 20	
20 < <i>t</i> ≤ 25	
25 < <i>t</i> ≤ 30	
30 < <i>t</i> ≤ 50	

(2) (Total 5 marks) 2. This histogram gives information about the books sold in a bookshop one Saturday.



(a) Use the histogram to complete the table.

Price (P) in pounds (£)	Frequency
$0 < P \leq 5$	
5 < <i>P</i> ≤ 10	
10 < <i>P</i> ≤ 20	
$20 < P \le 40$	

(2)

The frequency table below gives information about the books sold in a second bookshop on the same Saturday.

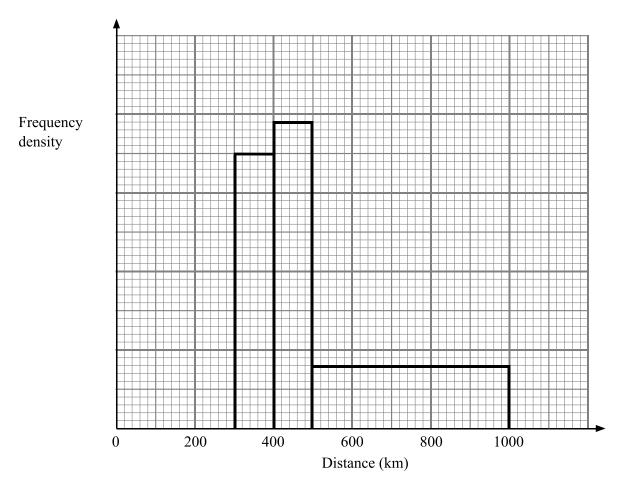
Price (P) in pounds (£)	Frequency
$0 < P \leq 5$	80
5 < <i>P</i> ≤ 10	20
10 < <i>P</i> ≤ 20	24
$20 < P \le 40$	96

(b) On the grid below, draw a histogram to represent the information about the books sold in the second bookshop.



(3) (Total 5 marks)

3. The incomplete table and histogram give some information about the distances walked by some students in a school in one year.



(a) Use the information in the histogram to complete the frequency table.

Distance (d) in km	Frequency
0 < <i>d</i> ≤ 300	210
300 < <i>d</i> ≤ 400	350
400 < <i>d</i> ≤ 500	
500 < <i>d</i> ≤ 1000	

(b) Use the information in the table to complete the histogram.

(1)

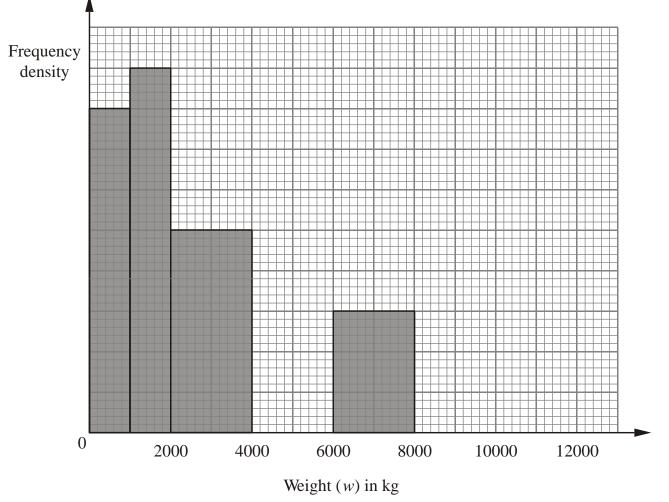
(2)

(Total 3 marks)

4. The incomplete histogram and table show information about the weights of some containers.

Weight (<i>w</i>) in kg	Frequenc y
0 < <i>w</i> ≤ 1000	16
1000 < <i>w</i> ≤ 2000	
$2000 < w \le 4000$	
$4000 < w \le 6000$	16
$6000 < w \le 8000$	
$8000 < w \le 12000$	8

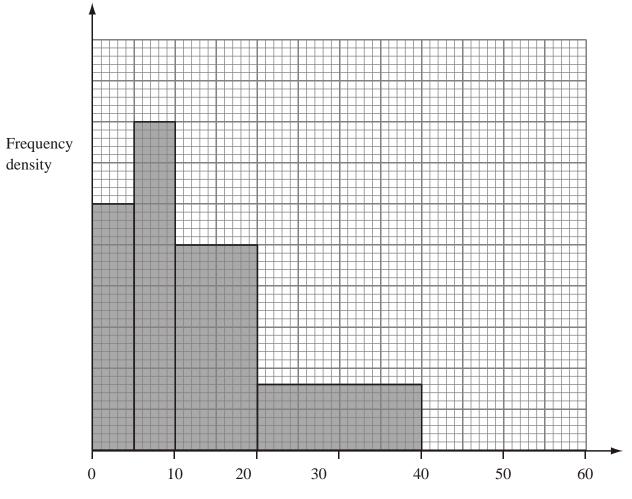
- (a) Use the information in the histogram to complete the table.
- (b) Use the information in the table to complete the histogram.



(2) (Total 4 marks)

(2)

5. The incomplete histogram and table give some information about the distances some teachers travel to school.



Distance (d km)

(a) Use the information in the histogram to complete the frequency table.

Distance (dkm)	Frequency
0 < <i>d</i> ≤ 5	15
5 < <i>d</i> ≤ 10	20
10 < <i>d</i> ≤ 20	
20 < <i>d</i> ≤ 40	
$40 < d \le 60$	10

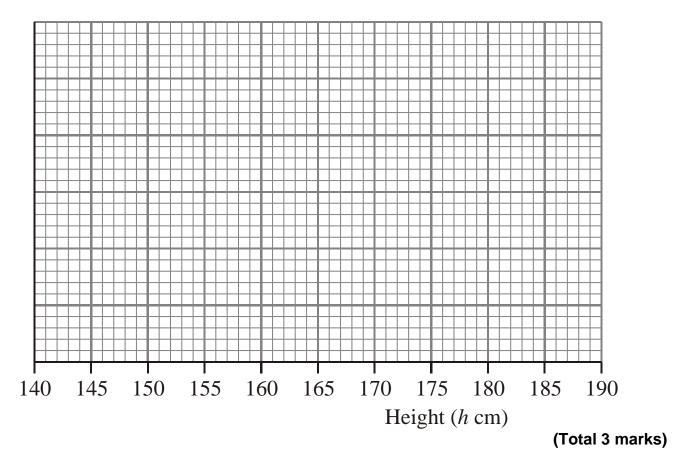
(2)

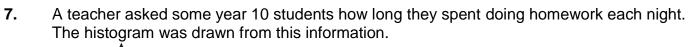
(b) Use the information in the table to complete the histogram.

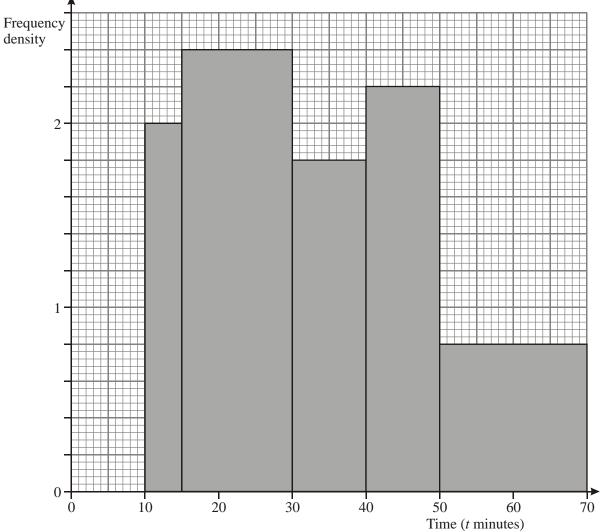
(1) (Total 3 marks) 6. The table gives information about the heights, in centimetres, of some 15 year old students.

Height (h cm)	145 < <i>h</i> ≤ 155	155 <i>< h</i> ≤ 175	175 < <i>h</i> ≤ 190
Frequency	10	80	24

Use the table to draw a histogram.







Use the histogram to complete the table.

Time (<i>t</i> minutes)	Frequency
10 ≤ <i>t</i> < 15	10
15 ≤ <i>t</i> < 30	
$30 \le t < 40$	
$40 \le t < 50$	
$50 \le t < 70$	

(Total 2 marks)

Moving Averages

Things to remember:

- In this context, averages means the mean (add the numbers and divide by how many there were.
- Moving averages are used to identify trends in data peaks, troughs, increasing and decreasing trends.

Questions:

1. The table shows the number of computer games sold in a supermarket each month from January to June.

	Jan	Feb	Mar	Apr	May	Jun
ĺ	147	161	238	135	167	250

Work out the three month moving averages for this information.

······

(Total 2 marks)

2. The table shows the number of digital cameras Bytes sold each month in the first six months of 2005.

Month	January	February	March	April	May	June
Number of digital cameras sold	30	19	20	15	27	39

The first 3-month moving average for this data is 23

Work out the **second** 3-month moving average for this data.

(Total 2 marks)

3. The table shows the number of orders received each month by a small company.

Month	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug
Number of								
orders	23	31	15	11	19	16	20	13
received								

Work out the first two 4-month moving averages for this data.

..... and (Total 3 marks) 4. A shop sells DVD players.

The table shows the number of DVD players sold in every three-month period from January 2003 to June 2004.

Year	Months	Number of DVD players sold		
2003	Jan – Mar	58		
	Apr – Jun	64		
	Jul – Sep	86		
	Oct – Dec	104		
2004	Jan – Mar	65		
	Apr – Jun	70		

- (a) Calculate the set of four-point moving averages for this data.
- (b) What do your moving averages in part (a) tell you about the trend in the sale of DVD players?
- 5. Paul and Carol open a new shop in the High Street. The table shows the monthly takings in each of the first four months.
 Month Jan Feb March April

Monthly takings (£)	9375	8907	9255	9420
Work out the 3-point	movina	average	s for this	informa

Work out the 3-point moving averages for this information.

(Total 2 marks)

6. The owner of a music shop recorded the number of CDs sold every 3 months. The table shows his records from January 2004 to June 2005.

Year	Months	Number of CDs
2004	Jan – Mar	270
	Apr – Jun	324
	Jul – Sept	300
	Oct – Dec	258
2005	Jan – Mar	309
	Apr – Jun	335

(a) Calculate the complete set of four-point moving averages for this information.

(b)	What trend do these moving averages suggest?	 	(2)
			 (1) 8 marks)

7. The table shows some information about student absences.

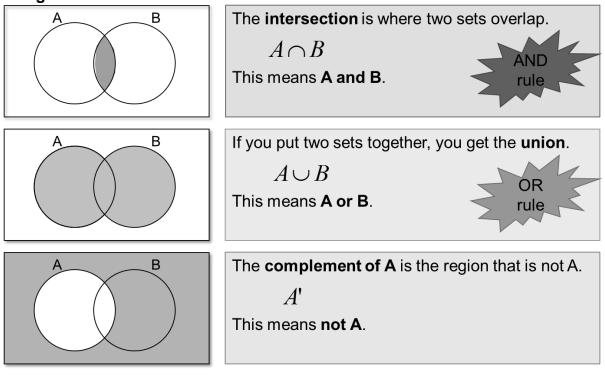
Term	Autumn		Summer			Summer	
	2003	2004	2004	2004	2005	2005	
Number of	408	543	351	435	582	372	
absences	-00	5-5	551	-55	502	512	

Work out the three-point moving averages for this information. The first two have been done for you.

434, 443,, **(Total 2 marks)**

Set Theory

Things to remember:



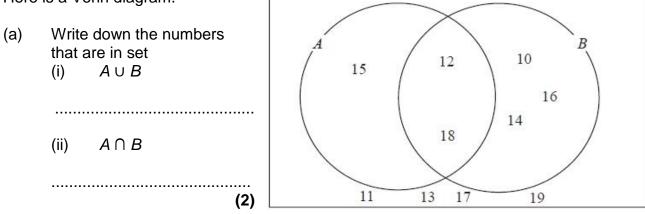
Questions:

1.

 $\mathcal{E} = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ $A = \{ \text{multiples of } 2 \}$ $A \cap B = \{2, 6\}$ $A \cup B = \{1, 2, 3, 4, 6, 8, 9, 10\}$ Draw a Venn diagram for this information.

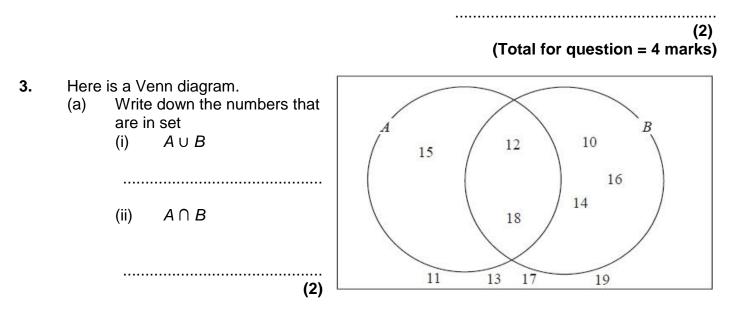
(Total for question is 4 marks)

2. Here is a Venn diagram.



One of the numbers in the diagram is chosen at random.

(b) Find the probability that the number is in set A'



One of the numbers in the diagram is chosen at random.

(b) Find the probability that the number is in set A'

(2) (Total for question = 4 marks)

- 4. Sami asked 50 people which drinks they liked from tea, coffee and milk. All 50 people like at least one of the drinks
 - 19 people like all three drinks.
 - 16 people like tea and coffee but do not like milk.
 - 21 people like coffee and milk.
 - 24 people like tea and milk.
 - 40 people like coffee.
 - 1 person likes only milk.
 - Sami selects at random one of the 50 people.
 - (a) Work out the probability that this person likes tea.

.....

(4)

(b) Given that the person selected at random from the 50 people likes tea, find the probability that this person also likes exactly one other drink.

(Total for question = 6 marks)

Proportion

Things to remember:

- Start by checking the question for squares, cubes and roots;
- "x is directly proportional to y" looks like x α y or x = ky
- "x is inversely proportional to y" looks like $\mathbf{x} \propto \frac{1}{y}$ or $\mathbf{x} = \frac{k}{y}$

Questions:

- **1.** The shutter speed, *S*, of a camera varies inversely as the square of the aperture setting, *f*. When f = 8, S = 125
 - (a) Find a formula for S in terms of f.

(b) Hence, or otherwise, calculate the value of S when f = 4

S =

(1) (Total 4 marks)

2. In a factory, chemical reactions are carried out in spherical containers. The time, *T* minutes, the chemical reaction takes is directly proportional to the square of the radius, *R* cm, of the spherical container. When R = 120, T = 32Find the value of *T* when R = 150

T =

(Total 4 marks)

	directly proportional to the square of <i>t</i> . 80 when <i>t</i> = 4 Express <i>d</i> in terms of <i>t</i> .	
(3)	Work out the value of d when $t = 7$	(b)
d =(1) d = 45	Work out the positive value of <i>t</i> when <i>d</i>	(c)
t =(2) (Total 6 marks) ctly proportional to the square of the time, <i>t</i> ,	distance, <i>D</i> , travelled by a particle is direct n. When $t = 40$, $D = 30$ Find a formula for <i>D</i> in terms of <i>t</i> .	
D =(3)	Calculate the value of D when $t = 64$	(b)
(1) nt figures.	Calculate the value of t when $D = 12$ Give your answer correct to 3 significan	(c)

..... (2) (Total 6 marks)

5. The time, T seconds, it takes a water heater to boil some water is directly proportional to the mass of water, m kg, in the water heater. When m = 250, T = 600

(a) Find T when m = 400

T =

(3) The time, T seconds, it takes a water heater to boil a constant mass of water is inversely proportional to the power, P watts, of the water heater. When P = 1400, T = 360Find the value of T when P = 900(b)

> *T* = (3)

(Total 6 marks)

- 6. A ball falls vertically after being dropped. The ball falls a distance *d* metres in a time of *t* seconds. *d* is directly proportional to the square of *t*. The ball falls 20 metres in a time of 2 seconds.
 - Find a formula for *d* in terms of *t*. (a)

<i>d</i> =	
(3	3)

Calculate the distance the ball falls in 3 seconds. (b)

> m (1)

Calculate the time the ball takes to fall 605 m. (C)

..... seconds

(3) (Total 7 marks)

- 7. In a spring, the tension (T newtons) is directly proportional to its extension (x cm). When the tension is 150 newtons, the extension is 6 cm.
 - (a) Find a formula for T in terms of x.

T =(3)

(b) Calculate the tension, in newtons, when the extension is 15 cm.

.....newtons (1)

(c) Calculate the extension, in cm, when the tension is 600 newtons.

.....cm (1) (Total 5 marks)

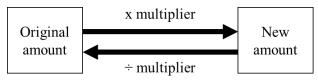
8. *f* is inversely proportional to *d*. When d = 50, f = 256Find the value of *f* when d = 80

f =(Total 3 marks)

Percentages – reverse

Things to remember:

Work out what the multiplier would have been; •



Questions:

Loft insulation reduces annual heating costs by 20%. 1. After he insulated his loft, Curtley's annual heating cost was £520. Work out Curtley's annual heating cost would have been, if he had not insulated his loft.

2. In a sale, normal prices are reduced by 20%. SALE - 20% OFF Andrew bought a saddle for his horse in the sale. The sale price of the saddle was £220. Calculate the normal price of the saddle.

£

£

(Total 3 marks)

(Total 3 marks)

- 3. Hajra's weekly pay this year is £240 This is 20% more than her weekly pay last year. Bill says 'This means Hajra's weekly pay last year was £192'. Bill is wrong, Explain why. (a)
 - (b) Work out Hajra's weekly pay last year.

£

(2) (Total 3 marks)

(1)

4. The price of all rail season tickets to London increased by 4%.
(a) The price of a rail season ticket from Cambridge to London increased by £121.60 Work out the price before this increase.

£

(b) After the increase, the price of a rail season ticket from Brighton to London was £2828.80

Work out the price before this increase.

£(3) (Total 5 marks)

 In a sale, normal prices are reduced by 25%. The sale price of a saw is £12.75 Calculate the normal price of the saw.

£

(Total 3 marks)

(2)

6. In a sale, normal prices are reduced by 12%. The sale price of a DVD player is £242. Work out the normal price of the DVD player.

£.....

(Total 3 marks)

A garage sells cars.
 It offers a discount of 20% off the normal price for cash.
 Dave pays £5200 cash for a car.
 Calculate the normal price of the car.

£

(Total 3 marks)

Useful websites:

www.mathswatchvle.com

(Video explanations and questions) Centre ID: twgash Username: firstname Password: lastname

www.methodmaths.com

(Past papers online that get instantly marked) Centre ID: wga Username: firstname Password: lastname

www.hegartymaths.com

(Online tutorials and quizzes) Login: first name and last name are case sensitive

www.bbc.co.uk/schools/gcsebitesize /maths

Remember: Do your best; it is all you can do 😳